

# Public Finance

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# Outline of the class

Introduction

Lecture 2: Tax incidence

**Lecture 3: Distortions and welfare losses**

Lecture 4-6: Optimal labor income taxation

# Efficiency cost of taxation

- Incidence: effect of policies on **distribution** of economic pie
- Efficiency or deadweight cost: effect of policies on **size** of the pie
- Focus in efficiency analysis is on quantities, not prices

- Government raises taxes for one of two reasons:
  - ① To raise revenue to finance public goods
  - ② To redistribute income
- But to generate \$1 of revenue, welfare of those taxed falls by more than \$1 because the tax distorts behavior
- How to implement policies that minimize these efficiency costs?
  - ▶ Start with positive analysis of how to measure efficiency cost of a given tax system

# Marshallian Surplus: Assumptions

- Simplest analysis of efficiency costs: Marshallian surplus
- Two assumptions:
  - ① Quasilinear utility: no income effects, money metric
  - ② Competitive production

# Partial Equilibrium Model: Setup

- Two goods:  $x$  and  $y$
- Consumer has wealth  $Z$ , utility  $u(x) + y$ , and solves

$$\max_{x,y} u(x) + y \text{ s.t. } (p + \tau)x + y = Z$$

- Firms use  $c(S)$  units of the numéraire  $y$  to produce  $S$  units of  $x$
- Marginal cost of production is increasing and convex:

$$c'(S) > 0 \text{ and } c''(S) \geq 0$$

- Firm's profit at pretax price  $p$  and level of supply  $S$  is

$$pS - c(S)$$

# Model: Equilibrium

- With perfect optimization, supply function for  $x$  is implicitly defined by the marginal condition

$$p = c'(S(p))$$

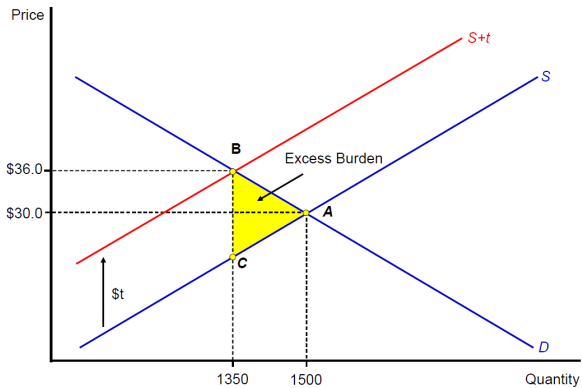
- Let  $\eta_S = p \frac{S'}{S}$  denote the price elasticity of supply
- Let  $Q$  denote equilibrium quantity sold of good  $x$
- $Q$  satisfies:

$$Q(\tau) = D(p) = S(p + \tau)$$

Let  $\eta_D = p \frac{D'}{D}$  denote the price elasticity of demand

- Consider effect of introducing a small tax  $d\tau > 0$  on  $Q$  and surplus

### Excess Burden of Taxation

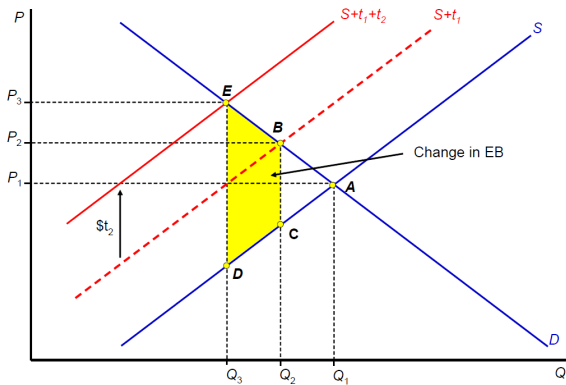




# Efficiency Cost: Qualitative Properties

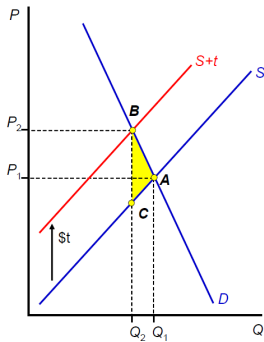
- ① Excess burden increases with square of tax rate
- ② Excess burden increases with elasticities

### EB Increases with Square of Tax Rate

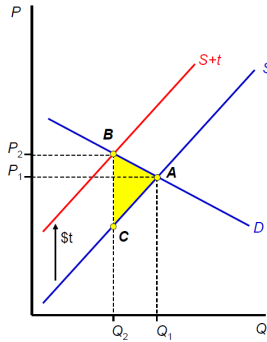


### Comparative Statics

(a) Inelastic Demand



(b) Elastic Demand



# Tax Policy Implications

- With many goods, the most efficient way to raise tax revenue is:
  - ① Tax inelastic goods more (e.g. medical drugs, food)
  - ② Spread taxes across all goods to keep tax rates relatively low on all goods (broad tax base)
- These are two countervailing forces; balancing them requires quantitative measurement of excess burden

# Measuring Excess Burden: Marshallian Surplus

- How to measure excess burden? Three empirically implementable methods:
  - ① In terms of supply and demand elasticities
  - ② In terms of total change in equilibrium quantity caused by tax
  - ③ In terms of change in government revenue

# Method 1: Supply and Demand Elasticities

Suppose there is no tax on the good and introduce a small tax  $d\tau > 0$  on  $Q$ . The excess burden is the size of the triangle:

$$\begin{aligned} EB &= -\frac{1}{2}dQd\tau \\ EB &= -\frac{1}{2}S'(p)dpd\tau = -\frac{1}{2}\underbrace{\frac{pS'}{S}}_{\eta_S} \frac{S}{p} \frac{\eta_D}{\eta_S - \eta_D} d\tau^2 \end{aligned}$$

since  $Q = S$ ,  $dQ = S'(p)dp$  and  $dp = (\frac{\eta_D}{\eta_S - \eta_D})d\tau$ . Therefore,

$$EB = -\frac{1}{2} \frac{\eta_S \eta_D}{\eta_S - \eta_D} pQ * \left( \frac{d\tau}{p} \right)^2$$

- Tax revenue  $R = Qd\tau$
- Useful expression is deadweight burden per dollar of tax revenue:

$$\frac{EB}{R} = -\frac{1}{2} \frac{\eta_S \eta_D}{\eta_S - \eta_D} \frac{d\tau}{p}$$

## Method 2: Distortions in Equilibrium Quantity

- Define  $\eta_Q = -\frac{dQ}{d\tau} \frac{p_0}{Q}$ ,  $p_0$  initial price,

where  $\eta_Q$  captures the effect of a 1 % increase in price via a tax change on equilibrium quantity, taking into account the endogenous price change (can be identified in the data).

Then,

$$\begin{aligned} EB &= -\frac{1}{2} \frac{dQ}{d\tau} d\tau d\tau \\ &= -\frac{1}{2} \frac{dQ}{d\tau} \left( \frac{p}{Q} \right) \left( \frac{Q}{p} \right) d\tau d\tau \\ &= \frac{1}{2} \eta_Q p Q \left( \frac{d\tau}{p} \right)^2 \end{aligned}$$

Reduced form effect of taxes on quantities (no need to have supply and demand elasticities).



# Marginal Excess Burden of Tax Increase

- First, excess burden of a tax  $\tau$  can be written as

$$EB(\tau) = -\frac{1}{2} \frac{dQ}{d\tau} \tau^2$$

- Now consider EB from raising tax by  $\Delta\tau$  given pre-existing tax  $\tau$ :

$EB(\Delta\tau) = EB(\tau + \Delta\tau) - EB(\tau)$ , assuming  $\frac{dQ}{d\tau}$  constant (demand curve locally linear)

$$\begin{aligned} EB(\Delta\tau) &= -\frac{1}{2} \frac{dQ}{d\tau} [(\tau + \Delta\tau)^2 - \tau^2] \\ &= -\frac{1}{2} \frac{dQ}{d\tau} \cdot [2\tau \cdot \Delta\tau + (\Delta\tau)^2] \\ &= -\tau \frac{dQ}{d\tau} \Delta\tau - \frac{1}{2} \frac{dQ}{d\tau} (\Delta\tau)^2 \end{aligned}$$

# Marginal Excess Burden of Tax Increase

So

$$EB(\Delta\tau) = -\tau \frac{dQ}{d\tau} \Delta\tau - \frac{1}{2} \frac{dQ}{d\tau} (\Delta\tau)^2$$

- First term is first-order in  $\Delta\tau$ ; second term is second-order  $((\Delta\tau)^2)$ .
- This is why taxing markets with pre-existing taxes generates larger marginal EB.

## Method 3: Leakage in government revenue

- To first order, marginal excess burden of raising  $\tau$  is:

$$\frac{\partial EB}{\partial \tau} = -\tau \frac{dQ}{d\tau}$$

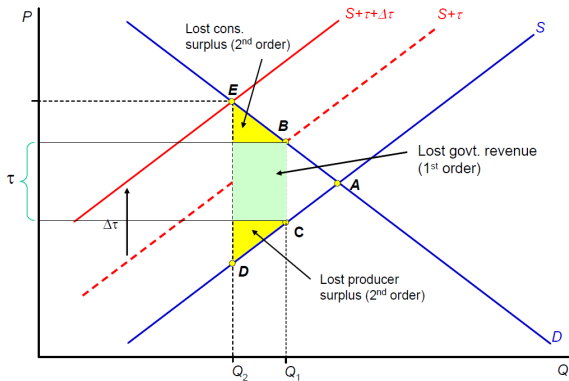
- Observe that tax revenue  $R(\tau) = Q\tau$ 
  - ▶ Mechanical revenue gain:  $\frac{\partial R}{\partial \tau}|_Q = Q$
  - ▶ Actual revenue gain:  $\frac{\partial R}{\partial \tau} = Q + \tau \frac{dQ}{d\tau}$
- MEB is the difference between mechanical and actual revenue gain:

$$\frac{\partial R}{\partial \tau}|_Q - \frac{dR}{d\tau} = Q - [Q + \tau \frac{dQ}{d\tau}] = -\tau \frac{dQ}{d\tau} = \frac{\partial EB}{\partial \tau}$$

# First vs. Second-Order Approximations

- Why does leakage in govt. revenue only capture first-order term?
  - ▶ Govt revenue loss: rectangle in Harberger trapezoid, proportional to  $\Delta\tau$ .
  - ▶ Consumer and producer surplus loss: triangles in trapezoid (proportional to  $\Delta\tau^2$ ).
- Method 3 is accurate for measuring marginal excess burden given pre-existing taxes but not introduction of new taxes.

### Excess Burden of a Tax Increase: Harberger Trapezoid



# General Model with Income Effects

- Drop quasilinearity assumption and consider an individual with utility

$$u(c_1, \dots, c_N) = u(c)$$

- Individual's problem:

$$\max_c u(c) \text{ s.t. } q \cdot c \leq Z$$

where  $q = p + \tau$  denotes vector of tax-inclusive prices and  $Z$  is wealth.

Labor can be viewed as commodity with price  $w$  and consumed in negative quantity.

# Demand Functions and Indirect Utility

- Let  $\lambda$  denote multiplier on budget constraint
- First order condition in  $c_i$ , for all  $i$ :

$$u_{c_i} = \lambda q_i$$

- These conditions implicitly define:
  - $c_i(q, Z)$ : the Marshallian (“uncompensated”) demand function
  - $v(q, Z)$ : the indirect utility function

# Measuring Deadweight Loss with Income Effects

- Question: how much utility is lost because of tax beyond revenue transferred to government?
- Marshallian surplus does not answer this question with income effects
  - ▶ Problem: not derived from utility function or a welfare measure
  - ▶ Creates various problems such as “path dependence” with taxes on multiple goods

$$\Delta CS(\tau^0 \rightarrow \tilde{\tau}) + \Delta CS(\tilde{\tau} \rightarrow \tau^1) \neq \Delta CS(\tau^0 \rightarrow \tau^1)$$

- Need units to measure “utility loss”
  - ▶ Introduce expenditure function to translate the utility loss into dollars (money metric).



# Expenditure Function

- Fix utility at  $U$  and prices at  $q$ : Find bundle that minimizes cost to reach  $U$  for  $q$ ,

$$e(q, U) = \min_c q \cdot c \text{ s.t. } u(c) \geq U$$

Let  $\mu$  denote multiplier on utility constraint, first order conditions given by:

$$q_i = \mu u_{c_i}$$

- These generate Hicksian (or compensated) demand functions:

$$c_i = h_i(q, u)$$

- Define individual's loss from tax increase as  $e(q^1, u) - e(q^0, u)$
- Single-valued function  $\rightarrow$  coherent measure of welfare cost, no path dependence.

# Compensating and Equivalent Variation

- But where should  $u$  be measured?
- Consider a price change from  $q^0$  to  $q^1$ .
- Utility at initial price  $q^0$ :

$$u^0 = v(q^0, Z)$$

- Utility at new price  $q^1$ :

$$u^1 = v(q^1, Z)$$

- Two concepts: compensating (CV) and equivalent variation (EV)  
use  $u^0$  and  $u^1$  as reference utility levels.

# Compensating Variation

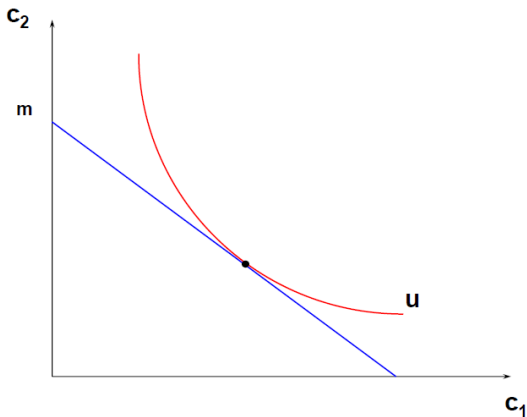
- Measures utility at initial price level ( $u^0$ ).
- Amount agent must be compensated in order to be indifferent about tax increase

$$CV = e(q^1, u^0) - e(q^0, u^0) = e(q^1, u^0) - Z.$$

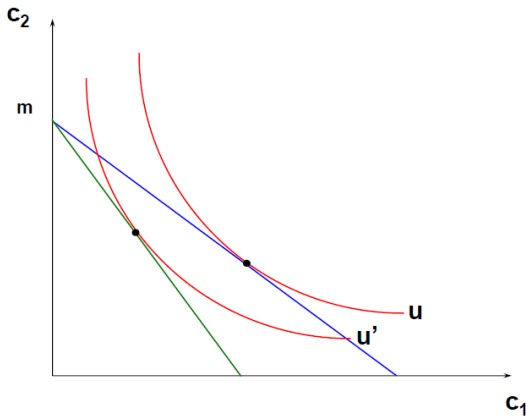
- How much compensation is needed to reach original utility level at *new* prices?
- CV is amount of ex-post cost that must be covered by government to yield same *ex-ante* utility:

$$e(q^0, u^0) = e(q^1, u^0) - CV.$$

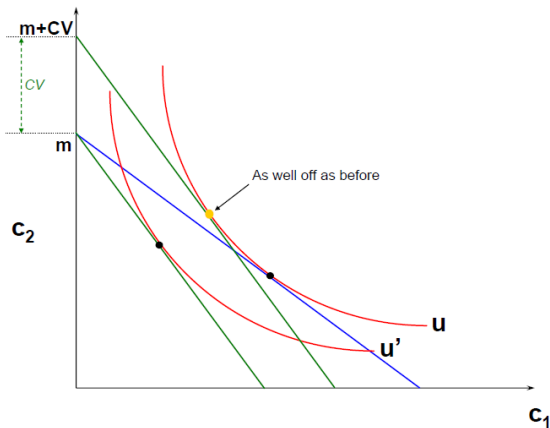
# Compensating Variation



# Compensating Variation: increase price of good 1



# Compensating Variation



# Equivalent Variation

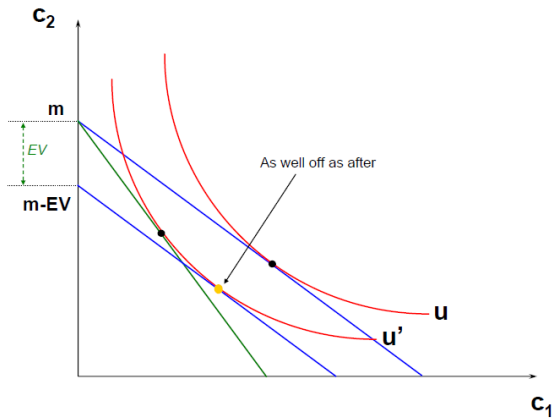
- Measures utility at new price level.
- Lump sum amount agent willing to pay to avoid tax (at pre-tax prices)

$$EV = e(q^1, u^1) - e(q^0, u^1) = Z - e(q^0, u^1).$$

- $EV$  is amount extra that can be taken from agent to leave him with same *ex-post* utility:

$$e(q^0, u^1) + EV = e(q^1, u^1).$$

# Equivalent Variation





# Efficiency Cost with Income Effects

- Goal: derive empirically implementable formula analogous to Marshallian EB formula in general model with income effects.
- Literature typically assumes either
  - ① Fixed producer prices and income effects;
  - ② Endogenous producer prices and quasilinear utility.
- With both endogenous prices and income effects, efficiency cost depends on how profits are returned to consumers.
- Formulas are very messy and fragile (Auerbach, 1985).

# Efficiency Cost Formulas with Income Effects

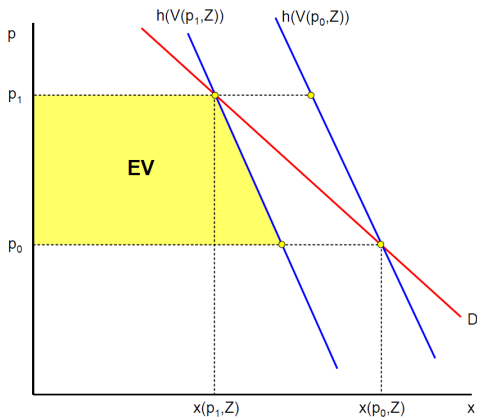
- Derive empirically implementable formulas using Hicksian demand ( $EV$  and  $CV$ ).
- Assume  $p$  is fixed  $\rightarrow$  flat supply, constant returns to scale.
- The envelope thm implies that  $e_{q_i}(q, u) = h_i$ , and so:

$$e(q^1, u) - e(q^0, u) = \int_{q^0}^{q^1} h(q, u) dq.$$

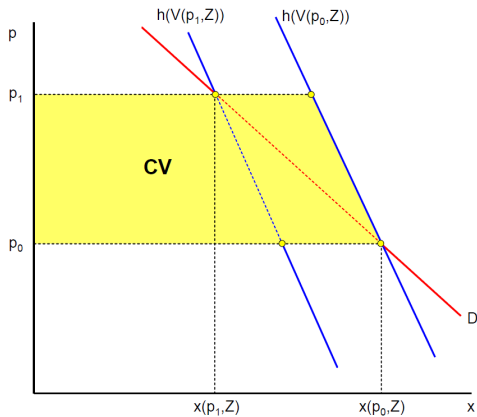
- If only one price is changing, this is the area under the Hicksian demand curve for that good.
- Note that optimization implies that

$$h(q, v(q, Z)) = c(q, Z)$$

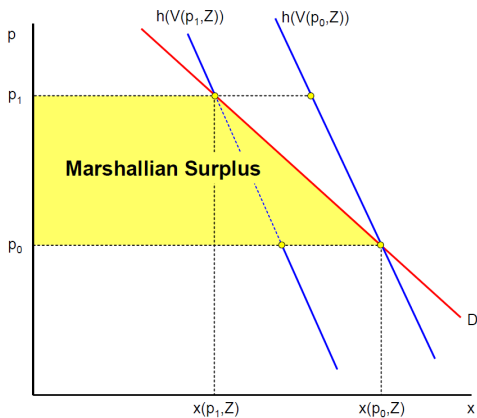
## Compensating vs. Equivalent Variation



## Compensating vs. Equivalent Variation



## Marshallian Surplus



# EV, CV, and Marshallian Surplus

- With one price change:

$$EV < \text{Marshallian Surplus} < CV$$

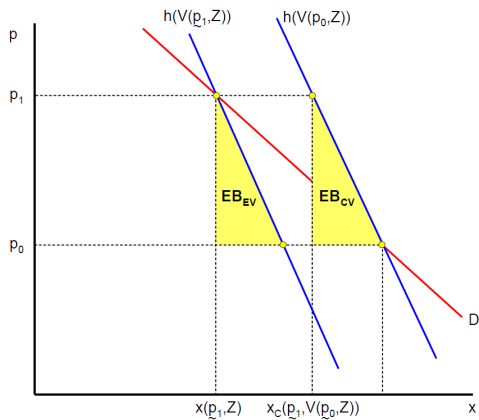
- But this is not true in general with multiple price changes because Marshallian Surplus is ill-defined

# Excess Burden

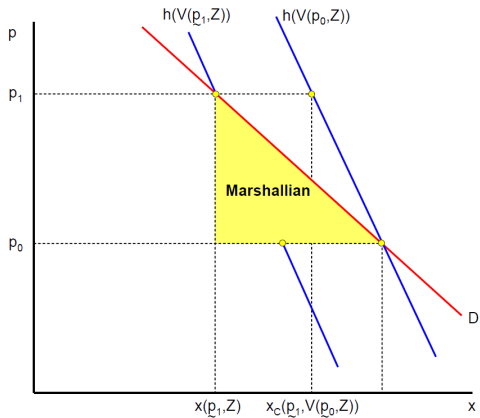
- Deadweight burden: change in consumer surplus less tax paid
- What is lost in excess of taxes paid?
- Two measures, corresponding to  $EV$  and  $CV$ :

$$EB(u^1) = EV - (q^1 - q^0)h(q^1, u^1) \text{ [Mohring 1971]}$$

$$EB(u^0) = CV - (q^1 - q^0)h(q^1, u^0) \text{ [Diamond and McFadden 1974]}$$







# Excess Burden

- In general,  $CV$  and  $EV$  measures of  $EB$  will differ
- Marshallian measure overstates excess burden because it includes income effects
  - Income effects are not a distortion in transactions
  - Buying less of a good due to having less income is not an efficiency loss
- $CV = EV = \text{Marshallian DWL}$  only with quasilinear utility (Chipman and Moore 1980)

# Implementable Excess Burden Formula

- Consider increase in tax  $\tau$  on good 1 to  $\tau + \Delta\tau$
- No other taxes in the system
- Recall the expression for  $EB$ :

$$EB(\tau) = [e(p + \tau, U) - e(p, U)] - \tau h_1(p + \tau, U)$$

- Second-order Taylor expansion:

$$\begin{aligned} MEB &= EB(\tau + \Delta\tau) - EB(\tau) \\ &\simeq \frac{dEB}{d\tau} \Delta\tau + \frac{1}{2} (\Delta\tau)^2 \frac{d^2EB}{d\tau^2} \end{aligned}$$

# Harberger Trapezoid Formula

$$\begin{aligned}\frac{dEB}{d\tau} &= h_1(p + \tau, U) - \tau \frac{dh_1}{d\tau} - h_1(p + \tau, U) \\ &= -\tau \frac{dh_1}{d\tau} \\ \frac{d^2EB}{d\tau^2} &= -\frac{dh_1}{d\tau} - \tau \frac{d^2h_1}{d\tau^2}\end{aligned}$$

- Standard practice in literature: assume  $\frac{d^2h_1}{d\tau^2} = 0$  (locally linear Hicksian); not necessarily well justified b/c it does not vanish as  $\Delta\tau \rightarrow 0$

$$\Rightarrow MEB = -\tau \Delta\tau \frac{dh_1}{d\tau} - \frac{1}{2} \frac{dh_1}{d\tau} (\Delta\tau)^2$$

- Formula equals area of “Harberger trapezoid” using Hicksian demands

# Harberger Formula

- Without pre-existing tax, obtain “standard” Harberger formula:

$$EB = -\frac{1}{2} \frac{dh_1}{d\tau} (\Delta\tau)^2$$

- General lesson: use compensated (substitution) elasticities to compute  $EB$ , not uncompensated elasticities.
- To implement empirically, estimate Marshallian price elasticity and income elasticity. Then apply Slutsky equation:

$$\underbrace{\frac{\partial h_i}{\partial q_j}}_{\text{Hicksian Slope}} = \underbrace{\frac{\partial c_i}{\partial q_j}}_{\text{Marshallian Slope}} + \underbrace{c_j \frac{\partial c_i}{\partial Z}}_{\text{Income Effect}}$$

# Excess Burden with Taxes on Multiple Goods

- Previous formulas apply to case with tax on one good
- With multiple goods and fixed prices, excess burden of introducing a new tax  $\tau_k$

$$EB = -\frac{1}{2}\tau_k^2 \frac{dh_k}{d\tau_k} - \sum_{i \neq k} \tau_i \tau_k \frac{dh_i}{d\tau_k}$$

- Second-order effect in own market, first-order effect from other markets with pre-existing taxes
- Complementarity between goods important for excess burden calculations
- Ex: with an income tax, minimize total DWL tax by taxing goods complementary to leisure (Corlett and Hague 1953)

# Efficiency Cost: Applications

- ❶ **[Income Taxation]** Feldstein (1995,1999); Chetty (2009); Gorodnichenko, Martinez-Vazquez, and Peter (2009)
- ❷ **[Housing Subsidy]** Poterba (1992)
- ❸ **[Diesel Fuel Taxation]** Marion and Muehlegger (2008)

# Welfare Analysis in Behavioral Models

- Formulas derived thus far rely critically on full optimization by agents in private sector
- How to calculate efficiency costs when agents do not optimize perfectly?
- Relates to broader field of behavioral welfare economics
- Two papers if you are interested:
  - ① Conceptual Issues: Bernheim and Rangel (2009)
  - ② Applied Welfare Analysis: Chetty, Looney, Kroft (2009)



# Behavioral Welfare Economics

- Abstractly, effect of policies on welfare are calculated in two steps
  - ① Effect of policy on behavior
  - ② Effect of change in behavior on utility
- Challenge: identifying (2) when agents do not optimize perfectly
  - How to measure objective function without tools of revealed preference?
  - Danger of paternalism

# Behavioral Welfare Economics: Two Approaches

- Approach #1: Build a positive model of deviations from rationality
  - Ex: hyperbolic discounting, bounded rationality, reference dependence
  - Then calculate optimal policy within such models
- Approach #2: Choice-theoretic welfare analysis (Bernheim and Rangel 2009)
  - Do not specify a positive model to rationalize behavior
  - Instead map directly from observed choices to statements about welfare
  - Analogous to “sufficient statistic” approach

# Behavioral Welfare Economics: Two Approaches

- Consider three different medicare plans with different copays:  $L, M, H$  and corresponding variation in premiums
- We have data from two environments:
  - ❶ On red paper,  $H > M > L$
  - ❷ On blue paper,  $M > H > L$

# Behavioral Welfare Economics: Two Approaches

- Approach 1: build a model of why color affects choice and use it to predict which choice reveals “true” experienced utility
- Approach 2: Yields bounds on optimal policy
  - $L$  cannot be optimal given available data irrespective of positive model
  - Optimal copay bounded between  $M$  and  $H$
- Key insight: no theory of choice needed to make statements about welfare
  - Do not need to understand why color affects choice

# Directions for Further Work on Behavioral Welfare Analysis

- ❶ Normative analysis of tax policy
  - ▶ Value of tax simplification
- ❷ Use similar approach to welfare analysis in other contexts
  - ▶ Design consumer protection laws and financial regulation in a less paternalistic manner by studying behavior in domains where incentives are clear

# Recent reappraisal: Saez and Zucman (2023)

- Provide information on the current distribution of income and tax payments
- Key to quantify income inequality and the direct effects of taxes
- They call it *distributional current-tax analysis*

Background: Conceptual setup for Distributional National Accounts (DINA), Piketty, Saez, Zucman (2018).

# Illustration: Two-factor model

Production:

- Aggregate production function  $Y = F(K, L)$
- Perfect competition
- $w$  = economy-wide pre-tax wage rate,  $r$  = pre-tax rate of return on capital
- Profits maximization:  $w = F_L$  and  $r = F_K$
- Assume CRS: zero profits  $F(K, L) = rK + wL$
- Denote by  $\sigma$  the elasticity of substitution between  $K$  and  $L$  and by  $\alpha = \frac{rK}{Y}$  the share of capital income in the economy.

## Supply side:

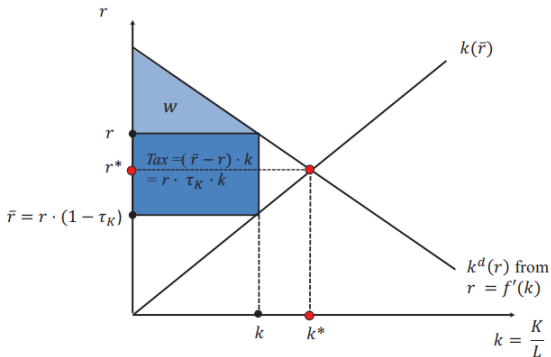
- Assume  $L$  is fixed
- Capital income taxed at  $\tau_k$
- Capital depends on the net-of-tax return  $\bar{r} = r(1 - \tau_K)$
- We can express everything in terms of capital per unit of labor  $k = K/L$ . As  $L$  is fixed, the supply of capital  $k = k(\bar{r})$  depends solely on  $\bar{r}$ .
- Define  $f(k) = F(1, K/L) = F(K, L)/L$  as output per unit of labor  
 $F_K = f'(k)$  and  $F_L = f(k) - kf'(k)$



The equilibrium conditions of the model are:

- $r = f'(k)$  (demand for capital)
- $w = f(k) - kf'(k) = \int_0^k f'(k)dk - rk$  (demand for labor)
- $k = k(r(1 - \tau_K))$  (supply of capital)

Figure 1: General Equilibrium with Capital Tax



Notes: The figure depicts the effect of a tax on capital income at rate  $\tau_K$  on the interest rate  $r$ , the capital to labor ratio  $k = K/L$ , and the wage  $w$  in a general equilibrium neoclassical model with fixed labor  $L$ , CRS production  $F(K, L) = L \cdot F(K/L, 1) = L \cdot f(k)$ . The equilibrium is characterized by 3 equations: (1)  $r = f'(k)$  (rate of return of capital equals its marginal return which generates the demand for capital  $k^d(r)$ ), (2)  $k = k(\bar{r})$  (capital supply depends on its net of tax return  $\bar{r} = r(1 - \tau_K)$ ), (3)  $w = f(k) - k f'(k) = \int_0^k f'(\kappa) d\kappa - rk$  (the wage  $w$  can be read as the area below the demand curve and above the  $r$  horizontal line). Without taxes, the equilibrium is  $(r^*, k^*)$ . With a tax rate  $\tau_K$ , the equilibrium shifts to  $(r, k)$ . The tax collects the rectangle,  $(r - \bar{r})k = \tau_K r k$ , it increases  $r$ , and reduces  $\bar{r}$  and  $w$ . The tax reduces the wage and the surplus of capitalists by an excess burden triangle  $\simeq (1/2) \cdot r \tau_K \cdot (k^* - k)$  over and above taxes collected. In this economy, pre-tax labor income is  $wL$ , pre-tax capital income is  $rK$ , and post-tax capital income is  $r(1 - \tau_K)K$ .

# Illustration to criticize distributional tax analysis carried out by government agencies

- Current tax analysis: pre-tax income of workers is  $w$   
Pre tax income of capitalists is  $rk$ , after tax income  $\bar{r}k$
- Conventional analysis: Pre-tax income of workers is  $w + (r - r^*)k$ : neither actual pre-tax income of workers  $w$ , nor counterfactual income if no tax.

# Empirical Welfare Analysis

Motivation: What government policies do the most to improve social welfare?

- Should we spend more (or less) on health insurance?
- Should we raise top marginal income tax rates?
- Should we invest more in children? At what age?

# Normative Evaluation of Policy Changes

- Discuss how to nest causal effects into a normative welfare framework
- Key idea: for each policy change, want to construct its implied **Marginal Value of Public Funds (MVPF)** :

$$MVPF = \frac{\text{Benefits to Recipients}}{\text{Net Govt Cost}}$$

- Hendren and Sprung-Keyser (2020): MVPF translates “reduced form” policy changes into statements about the social welfare impact of those policy changes

# MVPF Theory

- Define social welfare:

$$SWF = \sum_i \mu_i u_i$$

$u_i$  individual  $i$ 's utility function

$\mu_i$  individual  $i$ 's Pareto weight

- Define social marginal utility of income:  $\eta_i = \mu_i \lambda_i$  where  $\lambda_i$  is the private marginal utility of income

# Impact of Policy Change on Social Welfare

- Consider (small) policy change  $dp$ , e.g. change in tax rate, educ. subsidy, etc.
- First-order welfare impact:

$$\frac{dSWF}{dp} = \sum_i \mu_i \frac{du_i}{dp} = \bar{\eta}_p \sum_i WTP_i$$

- $\sum_i WTP_i$  is the sum of willingness to pay for the policy by beneficiaries, out of their own income, in \$
- $\bar{\eta}_p = \sum_i \mu_i \frac{WTP_i}{\sum_i WTP_i}$  is incidence-weighted average social marginal utility of income

# Reminder: Envelope Theorem

- Consider a parameterized maximization problem:

$$u(p) = \max_y u(y, p) = u(y^*(p), p)$$

- By the FOC, maximization means that when  $y = y^*(p)$ :

$$u_y(y, p) = 0$$

- By the chain rule for differentiation:

$$u'(p) = \underbrace{u_y(y^*(p), p)}_{=0} y^{*'}(p) + u_p(y^*(p), p)$$

and the envelope theorem just says this:

$$\frac{du}{dp} = u'(p) = u_p(y^*(p), p)$$



# Compare Policies by Normalizing by Cost

- Most policies ( $dp$ ) are not budget neutral
- Let  $R$  denote govt budget and  $G = \frac{dR}{dp}$  denote net impact on govt budget
- $G$  includes any fiscal externalities from behavioral responses to the policy

- The Marginal Value of Public Funds (MVPF) of policy  $p$  is given by:

$$MVPF_p = \frac{\sum_i WTP_i}{G} = \frac{\text{Willingness To Pay}}{\text{Govt Net Cost}}$$

- \$1 of govt spending on the policy delivers:

\$  $MVPF_p$  benefits to the beneficiaries of the policy

$\bar{\eta}_p MVPF_p$  in social welfare ( $= \frac{dSWF}{dp} / \frac{dR}{dp}$ )

# MVPF and Policies that Increase Welfare

- Take two (non-budget neutral) policies: policy 1 and policy 2
- Consider budget neutral policy,  $dp$ : increase spending on policy 1 financed from less spending (greater revenue) from policy 2
- To first order, combined policy increases social welfare ( $dSWF/dp > 0$ ) if only if:  $\bar{\eta}_1 MVPF_1 > \bar{\eta}_2 MVPF_2$
- MVPFs characterize price of delivering welfare to the beneficiaries through the policy

Motivates comparing policies with similar distributional incidence ( $\bar{\eta}_1 \approx \bar{\eta}_2$ )

Laffer effect occurs when  $WTP > 0$  and  $Net\ Cost < 0 \Rightarrow$   
 $MVPF = \infty$

# Example MVPF: Tax Rate Change

- Let's compute the MVPF a policy that reduces the marginal income tax rate,  $\tau$ , by  $d\tau$

- Let  $\tau$  denote the marginal tax rate on earnings  $y$ .

- Government revenue is  $R = \tau E[y]$

where  $E[y]$  is the average revenue subjected to the tax

- So, changing taxes leads to a change in revenue

$$\frac{dR}{d\tau} = E[y] + \tau \frac{dE[y]}{d\tau} = E[y](1 + \epsilon)$$

$\epsilon = \frac{dE[y]}{d\tau} \frac{\tau}{E[y]}$  is the elasticity of tax revenue with respect to the tax rate

- Depends on the causal effect of the tax change on tax revenue

- Now, consider the WTP
- Here's where the envelope theorem is useful
- If you earn \$ 100 and taxes go from 10 % to 9 %, WTP \$1 for the decrease regardless of how you change earnings (to first order)

$$\frac{1}{\lambda_i} \frac{du_i}{d\tau} = y_i$$

E.g., quasilinear  $u_i = \max_y y - \tau y - v_i(y)$

- So, average WTP is  $E[y]$  and the MVPF is given by

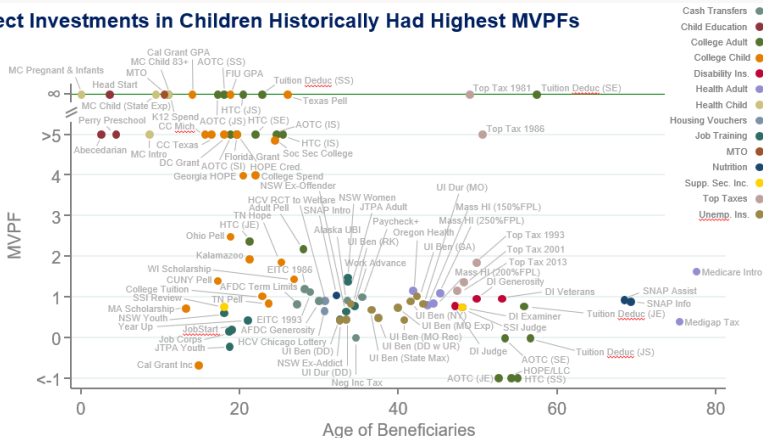
$$MVPF = \frac{E[y]}{E[y](1 + \epsilon)} = \frac{1}{1 + \epsilon}$$

- Key statistic: causal effect of changing tax rates on government revenue: For every \$1 of a tax cut, how much do individuals change their incomes

# Empirical Estimates of MVPFs for Various Policies

- Hendren and Sprung-Keyser (2020) construct 133 MVPFs for policies in social insurance, education and job training, taxes and cash transfers, and in-kind transfers.
- New MVPF estimates available at [www.policyimpacts.org](http://www.policyimpacts.org)
- Construct sample from survey and review articles in several policy domains
- Assess robustness to range of assumptions:
  - ▶ Program Parameters (discount rate, effective tax rate , etc.)
  - ▶ Forecasting/Extrapolation of Observed Effects
  - ▶ Validity of Empirical Designs (RCTs/RDs vs. Diff-in-Diff; Peer Reviewed vs. not; etc.)
  - ▶ Publication Bias (Andrews and Kasy, 2019)

## Direct Investments in Children Historically Had Highest MVPFs



# Link MVPF and MEB

- Marginal excess burden (MEB) corresponds to a distinct policy experiment
- Imagine doing the policy but closing the budget constraint through individual-specific lump-sum taxation (Auerbach and Hines, 2002)
- Rather than scaling up/down different policies to get to budget neutrality as in MVPF framework
- Requires compensated (Hicksian elasticities) not causal effect to calculate MEB



# MEB of Tax Rate Change

- Budget constraint is  $c \leq \tau y + t$ , where  $t$  is a lump-sum transfer
- Consider the revenue impact of a tax change that also rebates revenue through changing  $t$

$$\frac{dR}{d\tau^c} = \underbrace{E[y] + \tau \frac{dE[y]}{d\tau}}_{\text{Tax change}} - \underbrace{E[y] - \tau \frac{dE[y]}{dt}}_{\text{Lump-sum rebate}} = \tau \left( \frac{dE[y]}{d\tau} - \frac{dE[y]}{dt} \right)$$

- Normalizing by WTP,  $E[y]$ , we get

$$MEB = \epsilon^c$$

- $\epsilon^c$  denotes the compensated elasticity of tax revenue, subtracting the income effect  $\frac{dE[y]}{dt}$

# Two issues with the MEB Approach

1. Requires compensated, not causal effects

Income effects are hard to measure (especially if they are not invariant across environments)

2. Individual-specific transfers are not feasible (core idea behind Mirrlees' optimal income tax work: next set of slides)

# Outline of the class

Introduction

Lecture 2: Tax incidence

Lecture 3: Distortions and welfare losses

**Lecture 4-6: Optimal labor income taxation**